

INTERMEDIATE ALGEBRA

GPS # 18

5.2 MULTIPLICATIONS OF POLYNOMIALS

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Useful Definitions:

* To multiply polynomials, simply multiply each term of the first polynomial to each term of the other. Example: $(x^2 + 2x)(7x^2 - 5x + 3) = x^2(7x^2 - 5x + 3) + 2x(7x^2 - 5x + 3)$

* Special Products:

$$(x+y)(x-y) = x^2 - y^2$$

$$(x+y)^2 = x^2 + 2xy + y^2$$

$$(x-y)^2 = x^2 - 2xy + y^2$$

Note:

$$(x+y)^2 \neq x^2 + y^2$$

$$(x-y)^2 \neq x^2 - y^2$$

Handwritten signature/initials

Evaluate the following:

$$\begin{aligned} \text{a) } & (x^2 + 3x)(2x^2 + 3x + 1) \\ &= x^2(2x^2 + 3x + 1) + 3x(2x^2 + 3x + 1) \\ &= 2x^4 + 3x^3 + x^2 + 6x^3 + 9x^2 + 3x \\ &= 2x^4 + 9x^3 + 10x^2 + 3x \end{aligned}$$

$$\begin{aligned} \text{b) } & (2t-3)(4t-1) \\ &= 2t(4t-1) - 3(4t-1) \\ &= 8t^2 - 2t - 12t + 3 \\ &= 8t^2 - 14t + 3 \end{aligned}$$

see other method in back

$$\begin{aligned} \text{c) } & (x-5)(x-5) \\ &= x(x-5) - 5(x-5) \\ &= x^2 - 5x - 5x + 25 \\ &= x^2 - 10x + 25 \end{aligned}$$

(foil) $(x+2)(x-2)$
 $x^2 - 4$

$$\begin{aligned} \text{i) } & (x+2)^2 \Rightarrow (x+2)(x+2) \\ &= x^2 + 4x + 4 \end{aligned}$$

$$\begin{aligned} \text{k) } & (3-5x)^2 \\ &= 9 - 30x + 25x^2 \end{aligned}$$

$$\begin{aligned} \text{b) } & (2m+3)(m^2-3m-4) \\ &= 2m(m^2-3m-4) + 3(m^2-3m-4) \\ &= 2m^3 - 6m^2 - 8m + 3m^2 - 9m - 12 \\ &= 2m^3 - 3m^2 - 17m - 12 \end{aligned}$$

$$\begin{aligned} \text{d) } & (a-3)(a+3) \\ &= a(a+3) - 3(a+3) \\ &= a^2 + 3a - 3a - 9 \\ &= a^2 - 9 \end{aligned}$$

Inner to Inner & (foil) Outer to outer method

$$\begin{aligned} \text{e) } & (2p+8)(2p+8) \\ &= 4p^2 + 16p + 16p + 64 \\ &= 4p^2 + 32p + 64 \end{aligned}$$

$$\begin{aligned} \text{h) } & (3x-2)(x-4) \\ \text{(foil)} &= 3x^2 - 12x - 2x + 8 \\ &= 3x^2 - 14x + 8 \end{aligned}$$

$$\begin{aligned} \text{j) } & (3x-2)^2 \Rightarrow (3x-2)(3x-2) \\ &= 9x^2 - 12x + 4 \end{aligned}$$

$$\begin{aligned} \text{l) } & -2x(3x-2)^2 \\ &= -2x(9x^2 - 12x + 4) \\ &= 18x^3 + 24x^2 - 8x \end{aligned}$$