

**Useful Guidelines:**

- \* Quadratic Function:  $f(x) = ax^2 + bx + c, (a \neq 0)$ , where  $a, b$  and  $c$  are real numbers.
- \* The vertex of the graph of  $f(x) = ax^2 + bx + c, (a \neq 0)$  has coordinates  $(x, y) = \left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right)\right)$ .
- \* The axis of symmetry of the parabola has equation  $x = \frac{-b}{2a}$ .
- \* To graph a quadratic function:
  - Step 1: Determine whether the parabola opens up or down.
  - Step 2: Find the vertex.
  - Step 3: Find the  $x$ -intercepts (if any) and  $y$ -intercept.
  - Step 4: Plot the graph. [Find additional points as needed.]

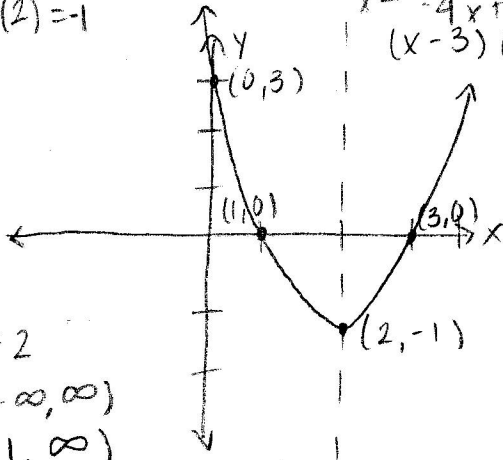
*no Grad  
in hlt.*

Graph each parabola, Give the vertex, axis, domain, and range.

1. a)  $f(x) = x^2 - 4x + 3$

$a=1$   $f(2) = (2)^2 - 4(2) + 3$   
 $b=-4$   $f(2) = -1$   
 $c=3$

$x=0$   $f(0) = 3$   
 $x^2 - 4x + 3 = 0$   
 $(x-3)(x-1)$

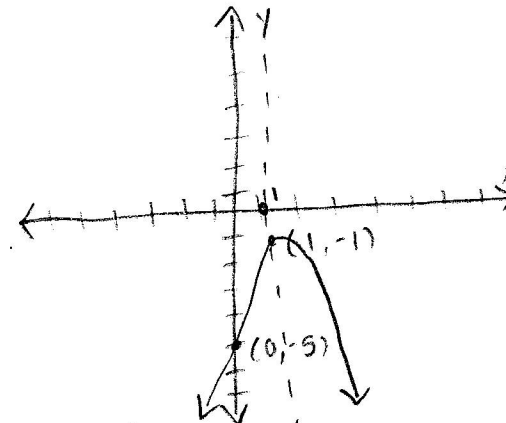


$V = (2, -1)$   
 $AOS = 2$   
 $x = \frac{-(-4)}{2(1)} = 2$   
 domain:  $[-\infty, \infty)$   
 range:  $[-1, \infty)$

b)  $f(x) = -4x^2 + 8x - 5$

$a=-4$   $f(1) = -4(1)^2 + 8(1) - 5$   
 $b=8$   $x=0$   $f(0) = -5$   
 $c=-5$

$x = \frac{-8}{2(-4)} = 1$



$V = (1, -1)$   
 $AOS = x = 1$   
 domain:  $[-\infty, \infty)$   
 range:  $[-\infty, -1]$

2. A rocket is fired upward. After  $t$  hour, the height of the rocket is given by  $S(t) = -2t^2 + 64t$ . Find the time required in hours for the rocket to reach maximum height, and find the maximum height in kilometers.

$a=-2$   $S(t) = -2t^2 + 64t$   
 $b=64$   
 $c=0$   
 $t = \frac{-64}{2(-2)} = \frac{-64}{-4} = 16$

$S(16) = -2(16)^2 + 64(16)$   
 $= 16 \text{ Hours}$   
 $= 512 \text{ Kilometers}$

3. The monthly total revenue for a beverage is given by  $R(x) = 4000x - 0.1x^2$  dollars, where  $x$  is the number of units sold.

a) To maximize the monthly revenue, how many units must be sold?

$a = -0.1$   $-4000$   
 $b = 4000$   
 $\frac{-4000}{2(-0.1)} = 20,000 \text{ units}$

b) What is the maximum possible monthly revenue?

$R(20,000) = 4000(20,000) - 0.1(20,000)^2 =$

$\$40,000,000$