

COLLEGE ALGEBRA

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 Class Time: 11:30 Date: 1-31-08

GPS #11

2.1 QUADRATIC FUNCTIONS; PARABOLAS

Useful Guidelines:

* Quadratic Function: $f(x) = ax^2 + bx + c, (a \neq 0)$, where a, b and c are real numbers.

* The vertex of the graph of $f(x) = ax^2 + bx + c, (a \neq 0)$ has coordinates $(x, y) = \left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right)\right)$.

20/20 Graded!

* The axis of symmetry of the parabola has equation $x = \frac{-b}{2a}$.

* To graph a quadratic function:

Step 1: Determine whether the parabola opens up or down.

Step 2: Find the vertex.

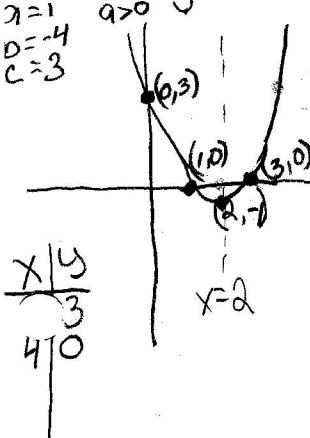
Step 3: Find the x -intercepts (if any) and y -intercept.

Step 4: Plot the graph. [Find additional points as needed.]

Graph each parabola, Give the vertex, axis, domain, and range. $ax^2 + bx + c$ $x = \frac{-b}{2a}$

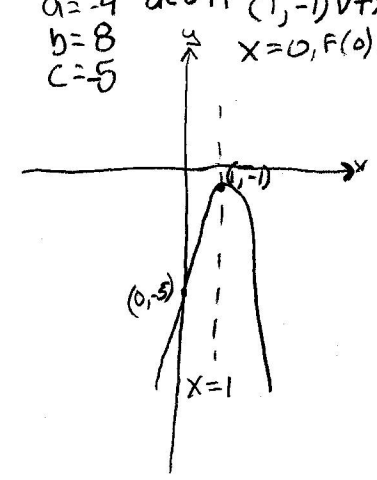
1. a) $f(x) = x^2 - 4x + 3$ $\frac{(-4)}{2(1)} x = 2$ $(2, -1) \vee x$

b) $f(x) = -4x^2 + 8x - 5$ $x = \frac{-8}{2(-4)} x = 1$



$D: (-\infty, \infty)$
 $R: [-1, \infty)$

$2^2 - 4(2) + 3 = -1$
 $x = 0, f(0) = 3$
 $x^2 - 4x + 3 = 0$
 $(x - 3)(x - 1) = 0$ $x = 1, 3$



$D: (-\infty, \infty)$
 $R: (-\infty, -1]$

2. A rocket is fired upward. After t hour, the height of the rocket is given by $S(t) = -2t^2 + 64t$. Find the time required in hours for the rocket to reach maximum height, and find the maximum height in kilometers.

$a = -2$ $a < 0$ $t = \frac{-64}{2(-2)}$ $t = 16 \text{ hours}$ $2(16)^2 + 64(16)$ $-512 + 1024$ $mh = 512 \text{ km}$
 $b = 64$
 $c = 0$

3. The monthly total revenue for a beverage is given by $R(x) = 4000x - 0.1x^2$ dollars, where x is the number of units sold.

a) To maximize the monthly revenue, how many units must be sold?
 $a = -0.1$ $b = 4000$ $a < 0$
 $\frac{-4000}{2(-0.1)} x = 20000$
 $\frac{-b}{2a} = \frac{-4000}{2(-0.1)}$ $x = 20000 \text{ units}$

b) What is the maximum possible monthly revenue?
 $4000(20000) - 0.1(20000)^2 = 40,000,000$
 $80,000,000 - 40,000,000 = \$40,000,000$

So neat!