

Useful Guidelines:

The solutions of $ax^2 + bx + c = 0 (a \neq 0)$ are given by $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. "Quadratic Formula"

2y Cab
W NB!

If a , b , and c are integers, then the number and type of solutions can be predicted as follows:

- * If the discriminant $b^2 - 4ac > 0$, then we'll have two real solutions.
- * If the discriminant $b^2 - 4ac = 0$, then we'll have only one real solution.
- * If the discriminant $b^2 - 4ac < 0$, then we'll have two complex solutions.

1. Solve each equation using the quadratic formula and give the solution set.

a) $x^2 - x - 12 = 0$

$a=1$
 $b=-1$
 $c=12$

$$\frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(-12)}}{2(1)}$$

$$= \frac{1 \pm \sqrt{1+48}}{2} = \frac{1 \pm \sqrt{49}}{2} = \frac{1 \pm 7}{2}$$

Solution set:
 $\left\{ \frac{1+7}{2}, \frac{1-7}{2} \right\} = \{4, -3\}$ OR $\{x \mid x = 4, -3\}$

b) $2x^2 - 3x + 3 = 0$

$a=2$
 $b=-3$
 $c=3$

$$\frac{-(-3) \pm \sqrt{(-3)^2 - 4(2)(3)}}{2(2)}$$

$$= 3 \pm \sqrt{9-24} = 3 \pm \sqrt{-15}$$

$$= 3 \pm i\sqrt{15}$$

Solution set:
 $\left\{ x \mid x = \frac{3+i\sqrt{15}}{4}, x = \frac{3-i\sqrt{15}}{4} \right\}$

2. Use the discriminant to predict whether the solutions to each equation are

A. one real solution; B. two real solutions; C. two complex solutions.

a) $x^2 + 5x + 4 = 0$

$(5)^2 - 4(1)(4)$
 $25 - 16 = 9$
 $9 > 0$, so
B. TWO real solutions

b) $2x^2 - 4x + 2 = 0$

$(-4)^2 - 4(2)(2)$
 $16 - 16 = 0$
 $0 = 0$, so
A. one real solution.

c) $5x^2 - 3x + 7 = 0$

$(-3)^2 - 4(5)(7)$
 $9 - 140 = -131$
 $-131 < 0$ so,
C. TWO complex solutions

d) $x^2 + 3x - 1 = 0$

$(3)^2 - 4(1)(-1)$
 $9 + 4 = 13$
 $13 > 0$ so,
B. TWO real solutions

3. If a ball is thrown upward at 32 feet per second from a height of 6 feet, the height of the ball can be modeled by $S(t) = 6 + 32t - 8t^2$ feet, where t is the number of seconds after the ball is thrown. How long after the ball is thrown is the height 36 feet?

$S(t) = 6 + 32t - 8t^2$
 $36 = 6 + 32t - 8t^2$
 $8t^2 - 32t + 30 = 0$
 $2(4t^2 - 16t + 15) = 0$
 $4t^2 - 16t + 15 = 0$

$a=4$
 $b=-16$
 $c=15$
vertex = 16

$(2t-3)(2t-5) = 0$

Solution set:
 $\left\{ \left(\frac{3}{2}, \frac{5}{2} \right) \right\}$

$42 > 0 =$ TWO real solutions