

**Useful Guidelines:**

- \* **One-to-one function:** A function whose inverse is also a function. [If  $x_1 \neq x_2$ , then  $f(x_1) \neq f(x_2)$ ]
- \* **Horizontal-line test:** If every horizontal line intersects the graph of  $f$  in at most one point, then  $f$  is one-to-one.
- \* The graph of a function  $f$  and its inverse  $f^{-1}$  (read as  $f$  inverse) are symmetric with respect to the line  $y = x$ .
- \* To find the inverse,  $f^{-1}(x)$ , of a one-to-one function:
  - (1) Let  $y = f(x)$
  - (2) Swap the variables  $x$  and  $y$
  - (3) Solve for  $y$  and replace  $y$  by  $f^{-1}(x)$
  - (4) Check the result by showing that  $f^{-1}(f(x)) = x$  and  $f(f^{-1}(x)) = x$
- \* To find the range of a one-to-one function  $f$ , find the domain of the inverse function  $f^{-1}$ .  
 [Domain of  $f$  = Range of  $f^{-1}$ ; Range of  $f$  = Domain of  $f^{-1}$ .]

$\frac{16}{20}$   $\text{E}$

1. Given  $f(x) = 50x$  and  $g(x) = \frac{x}{50}$ , find the following:

a)  $f(g(x)) = f\left(\frac{x}{50}\right) = 50\left(\frac{x}{50}\right) = x$

b)  $g(f(x)) = g(50x) = \frac{50x}{50} = x$

Determine whether the pair of functions  $f$  and  $g$  are inverses of each other.

?

2. If  $f(x) = 50x^3 - 18$  and  $g(x) = \sqrt[3]{\frac{x+18}{50}}$ , find the following:

a)  $f(g(x)) = f\left(\sqrt[3]{\frac{x+18}{50}}\right) = 50\left(\sqrt[3]{\frac{x+18}{50}}\right)^3 - 18 = x$

b)  $g(f(x)) = g(50x^3 - 18) = \sqrt[3]{\frac{(50x^3 - 18) + 18}{50}} =$

Determine whether  $f(x)$  and  $g(x)$  are inverse functions.

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3. Determine the function is one-to-one. If it is one-to-one, find a formula for its inverse and check the result by showing that  $f^{-1}(f(x)) = x$  and  $f(f^{-1}(x)) = x$

$f(x) = \frac{7}{x}$   $f^{-1}(x) = f\left(\frac{7}{x}\right) = \frac{7}{\frac{7}{x}} = x$

yes one-to-one

1. Let  $y = \frac{7}{x}$

4. Replace  $y$  with  $f^{-1}(x)$

2. swap  $x = \frac{7}{y}$

$f^{-1}(x) = \frac{7}{x}$

3. solve  $y$ :  $y = \frac{7}{x}$