

COLLEGE ALGEBRA

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GPS #24 2.8 ADDITIONAL EQUATIONS AND INEQUALITIES II

Useful Guidelines:

- * To solve an equations with radicals:
 - Step 1: Isolate one radical term on one side of the equation.
 - Step 2: Raise both sides of the equation to a power that is the same as the index of the radical.
 - Step 3: Solve the resulting equation; if it still contains a radical, repeat step 1 and step 2.
 - Step 4: Check all potential solutions in the original equation.
 - * To solve a quadratic inequality:
 - Step 1: Write the inequality as a quadratic equation and solve.
 - Step 2: Use the numbers solved from step 1 to divide a number line into intervals.
 - Step 3: Substitute a test number from each interval into the original inequality to determine the solution set.
- [Note: You need to consider the end points separately.]

*20/20
 Great job!*

Solve each equation.

1. a) $(\sqrt{3x+1})^2 = (4)^2$
 $3x+1 = 16$
 $3x = 15$
 $x = 5$

b) $\sqrt{x-12} - 8 = 0$
 $\sqrt{x-12} = 8$
 $x-12 = 64$
 $x = 76$

2. a) $\sqrt{2y+6} - 8 = -4$
 $\sqrt{2y+6} = 4$
 $2y+6 = 16$
 $2y = 10$
 $y = 5$

b) $(\sqrt[3]{m+7})^3 = (\sqrt[3]{3m-21})^3$
 $m+7 = 3m-21$
 $7 = 2m-21$
 $28 = 2m$
 $m = 14$

3. a) $(x+6)^{3/2} = (25)^{3/2} = (5^2)^{3/2}$
 $x+6 = 125$
 $x = 119$

b) $(w-8)^{4/3} = (8)^{4/3}$
 $w-8 = 16$
 $w = 24$

v. neat!

4. Solve each inequality and graph the solution set.

a) $x^2 - 2x - 15 > 0$ *vertex at (1, -16)*

$A=1$
 $B=-2$
 $C=-15$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-2) \pm \sqrt{4 + 60}}{2} = \frac{2 \pm 8}{2}$
 $x = 5, -3$

$f(x) = 1 - 2 - 15 = -16$
 vertex = $(1, -16)$

$(x+3)(x-5) < 0$
 $x+3=0 \Rightarrow x=-3$
 $x-5=0 \Rightarrow x=5$

x-intercept

b) $4t^2 - 48t + 80 \leq 0$ *less than zero you look at negatives*

$A=4$
 $B=-48$
 $C=80$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{48 \pm \sqrt{2304 - 1280}}{8} = \frac{48 \pm 32}{8}$
 $x = 10, 2$

$4(6)^2 - 48(6) + 80 = -64$
 vertex = $(6, -64)$

$4(t^2 - 12t + 20) = 0$
 $t^2 - 12t + 20 = 0$
 $(t-10)(t-2) = 0$
 $t = 10, t = 2$

solution set: [2, 10]