

## Useful Guidelines:

- \* An exponential function:  $f(x) = a^x$ , where  $a > 0$  and  $a \neq 1$ . The domain of  $f$  is the set of all real numbers.  
 [Note that the base is a constant and the exponent is a variable.]  $e = 2.718281828\dots$
- \* Properties of the Exponential Function  $f(x) = a^x$  (where  $a > 0$  and  $a \neq 1$ ):
- (1) Domain: the interval  $(-\infty, \infty)$ ; Range: the interval  $(0, \infty)$ ;
  - (2)  $x$ -intercepts: none;  $y$ -intercept: 1;
  - (3) Horizontal asymptote:  $y = 0$  as  $x \rightarrow -\infty$ ;
  - (4)  $f(x) = a^x$ ,  $a > 1$ , is an increasing, one-to-one, smooth and continuous function;  
 $f(x) = a^x$ ,  $0 < a < 1$ , is a decreasing, one-to-one, smooth and continuous function;
  - (5) The points  $(0,1)$ ,  $(1,a)$ , and  $(-1,\frac{1}{a})$  are always on the graph of  $f$ .

1. Evaluate  $f(x) = 3^x$  at  $x = -2, -1, 0, 1, 2$ , and 3. Graph the exponential function.

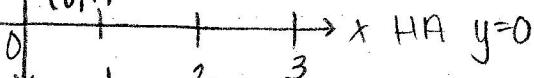
$x$	$f(x)$
-2	$3^{-2} = \frac{1}{9}$
-1	$3^{-1} = \frac{1}{3}$
0	$3^0 = 1$
1	$3^1 = 3$
2	$3^2 = 9$
3	$3^3 = 27$



$$a^{-n} = \frac{1}{2^n}$$

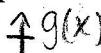
$$D: (-\infty, \infty)$$

$$R: (0, \infty)$$



2. Evaluate  $g(x) = \left(\frac{1}{3}\right)^x$  at  $x = -2, -1, 0, 1, 2$ , and 3. Graph the exponential function.

$x$	$g(x)$
-2	9
-1	3
0	1
1	$\frac{1}{3}$
2	$\frac{1}{9}$
3	$\frac{1}{27}$



$$D: (-\infty, \infty)$$

$$R: (0, \infty)$$

so decay!

3. Graph each function and determine the  $y$ -intercept, domain, range, and horizontal asymptote of  $f$ .

(a)  $f(x) = 3^{-x} - 2$

$$= \frac{1}{3^x} - 2$$

$x$	$f(x)$
-1	1
0	-1
1	$-\frac{5}{3}$

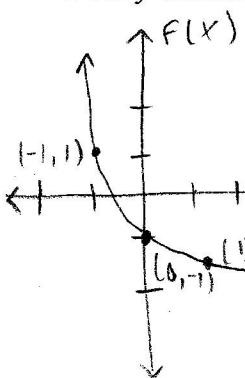
$$y\text{-int} = -1$$

$$d: (-\infty, \infty)$$

$$r: (-2, \infty)$$

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$$HA = y = -2$$



(b)  $f(x) = e^x$

$x$	$f(x)$
-1	$\frac{1}{e}$
0	1
1	$e$

$$y\text{-int} = 1$$

$$d: (-\infty, \infty)$$

$$r: (0, \infty)$$

$$HA = u = 0$$