

**Useful Guidelines:**

- \* Future value of an investment with continuous Compounding:  
If  $P$  is the amount invested at an interest rate  $r$  per year, the future value  $S$  at the end of  $t$  years is  
 $S = Pe^{rt}$ , with continuous compounding.
- \* The interest earned on an investment is the future value minus the original investment.

*ry Good*

1. Suppose that  $P$  is invested in CD account in which interest  $r$  is compounded continuously at 6% per year. The amount  $A$  accumulated after  $t$  years is  $A = Pe^{rt}$ . Find  $A$  if \$4000 is invested for

a) 6 years

b) 20 years

$$P = \$4,000$$

$$r = 0.06$$

$$t = 6 \text{ years}$$

$$S = Pe^{rt}$$

$$S = 4000e^{(0.06)(6)}$$

$$S = 4000e^{(1.36)} \quad \boxed{S = \$5,733.32}$$

$$P = \$4000$$

$$r = 0.06$$

$$t = 20 \text{ years}$$

$$S = Pe^{rt}$$

$$S = 4000e^{(0.06)(20)}$$

$$S = 4000e^{(1.2)}$$

$$\boxed{S = \$13,280.47}$$

2. a) What is the future value of \$2000 invested for 10 years at 9% compounded continuously?  
b) How much will be earned on this investment?

a)  $P = 2000$

$$r = 0.09$$

$$t = 10 \text{ years}$$

$$S = Pe^{rt}$$

$$S = 2000e^{(0.09)(10)}$$

$$S = 2000e^{(0.90)}$$

$$\boxed{S = \$4919.21}$$

b)  $4919.21$

$$- 2000.00$$

$$\boxed{\$2919.21}$$

*So neat!*

4. Suppose that \$250,000 is invested at 8% interest.

a) Find the amount of money in the account after 8 years if the interest is compounded annually.

b) Find the amount of money in the account after 8 years if the interest is compounded continuously.

a)  $S = P(1+r)^t$

$$P = 250,000$$

$$r = 0.08$$

$$t = 8 \text{ years}$$

$$S = P(1+r)^t$$

$$S = 250,000(1+0.08)^8$$

$$\boxed{S = \$462,732.55}$$

b)  $S = Pe^{rt}$

$$P = 250,000$$

$$r = 0.08$$

$$t = 8 \text{ years}$$

$$S = Pe^{rt}$$

$$S = 250,000e^{(0.08)(8)}$$

$$S = 250,000e^{(0.64)}$$

$$\boxed{S = \$474,120.22}$$