

COLLEGE ALGEBRA

GPS # 35 4.3 SOLUTION OF POLYNOMIAL EQUATIONS

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Useful Guidelines:

Greatest Common Factor: The largest common term that can be factor out from the polynomial.

For example: $3xy^2 + 6x = 3x(y^2 + 2)$, where $3x$ is the Greatest Common Factor.

Factoring by grouping:

Step 1: Group the terms so that each group has a common factor.

For example: $6x - 6y + 2x - 2y = (6x - 6y) + (2x - 2y)$

Step 2: Factor out the common factor in each group.

For example: $(6x - 6y) + (2x - 2y) = 6(x - y) + 2(x - y)$

Step 3: Factor out the common factor from the groups, if possible. Otherwise, try a different grouping.

For example: $6(x - y) + 2(x - y) = (x - y)(6 + 2) = 8(x - y)$

no good no!

1. Factor out the greatest common factor. Simplify the factors, if possible.

a) $x^2y - 3xy = xy(x - 3)$

b) $6p^2q^3 - 12pq = 6pq(pq^2 - 2)$

c) $(p - 2)(p + 2) - (p + 4)(p + 2) = (p + 2)[(p - 2) - (p + 4)] = -6(p + 2) = -6p - 12$

d) $(x - 3)(y + 2) - (x + 4)(y + 2) = (y + 2)[(x - 3) - (x + 4)] = (y + 2)[x - 3 - x - 4] = -7(y + 2) = -7y - 14$

2. Factor by grouping and simplify the factors, if possible.

a) $(3x + 3y) + (7x + 7y) = 3(x + y) + 7(x + y) = 10(x + y) = 10x + 10y$

b) $(15a + 3n) + (5ab + nb) = 3(5a + n) + b(5a + n) = (3 + b)(5a + n)$

c) $(30 + 5x) + (18y + 3xy) = 5(6 + x) + 3y(6 + x) = (5 + 3y)(6 + x)$

d) $(2ab - 2b) + (-a) = 2b(a - 1) + (-1)(a - 1) = (2b - 1)(a - 1)$

3. Solve the polynomial equation by factoring and give the solution set.

a) $3x^3 - 12x = 0$

$3x(x^2 - 4) = 0$

$3x = 0$ or $x^2 - 4 = 0$

$x = 0$ $(x - 2)(x + 2) = 0$

$x = 2$ or $x = -2$

$x = \pm 2$

Sol set: $\{x | x = 0 \text{ or } x = \pm 2\}$

b) $(4m^3 + m^2) - (16m - 4) = 0$

$m^2(4m + 1) - 4(4m + 1) = 0$

$m^2 - 4 = 0$ or $4m + 1 = 0$

$m = \pm 2$ or $m = -\frac{1}{4}$

Sol set: $\{-2, 2, -\frac{1}{4}\}$

<http://faculty.valenciac.edu/ashaw/>