

*no Grad
no PhD*

Useful Guidelines:

- * Square Root and Cube Root: The cube root function is defined for all inputs, whereas the square root function is defined only for nonnegative inputs.
- * Square Root Property: If k is a nonnegative numbers and $x^2 = k$, then $x = \pm\sqrt{k}$.
- * Solve Equations with Cube Roots: The solution to the equation $x^3 = k$ is $x = \sqrt[3]{k}$.
- * Power function: $f(x) = x^p$, where p is a rational number.
- * Root function: $f(x) = \sqrt[n]{x}$, where $n \geq 2$.

1. Use the square root property to solve each equation and give the solution set.

a) $x^2 = 49$
 $x = \pm \sqrt{49}$
 $x = \pm 7$
 $\{ -7, 7 \}$

b) $x^2 - 8 = 0$
 $x^2 = 8$
 $x = \pm 2\sqrt{2}$
 $\{ -2\sqrt{2}, 2\sqrt{2} \}$
 $\{ x | x = \pm 2\sqrt{2} \}$

c) $(x-4)^2 = 25$
 $x-4 = \pm 5$
 $x = 9$ or $x = -1$
 $\{ -1, 9 \}$

d) $(2x-5)^2 = 12$
 $2x-5 = \pm 2\sqrt{3}$
 $2x = \frac{5 \pm 2\sqrt{3}}{2}$
 $x = 2.5 \pm \sqrt{3}$
 $\{ x | x = 2.5 \pm \sqrt{3} \}$

2. Use the cube roots to solve each equation and give the solution set.

a) $2x^3 - 250 = 0$
 $\frac{2x^3}{2} = \frac{250}{2}$
 $x^3 = 125$
 $x = \sqrt[3]{125}$
 $x = 5$
 $\{ x | x = 5 \}$

b) $\sqrt[3]{(y-1)^3} = \sqrt[3]{8}$
 $y-1 = 2$
 $y = 3$
 $\{ y | y = 3 \}$

3. Solve the polynomial equation by using the root method and give the solution set.

a) $x^3 - 60 = 4$
 $\sqrt[3]{x^3} = \sqrt[3]{64}$
 $x = 4$
 $\{ x | x = 4 \}$

b) $6x^4 - 24x^2 = 0$
 $6x^2(x^2 - 4) = 0$
 $6x^2 = 0$ or $x^2 - 4 = 0$
 $x = 0$ $(x-2)(x+2)$
 $x = \pm 2$
 $\{ x | x = 0 \text{ or } x = \pm 2 \}$