

# COLLEGE ALGEBRA

GPS #38

## 4.5 RATIONAL FUNCTIONS AND RATIONAL EQUATIONS II

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Class Time: 11:30 A.M Date: 4/8/08

### Useful Guidelines:

To analyze the graph of a rational function,  $R(x) = \frac{p(x)}{q(x)}$ , in lowest terms:

- \* Step 1: Find the domain of the rational function.
- \* Step 2: Find the  $x$ -intercept(s), if any (let  $p(x) = 0$  when  $R(x)$  is in lowest term), and the  $y$ -intercept(s),  $R(0)$ .
- \* Step 3: Write  $R$  in lowest term and find the real zeros of the denominator (vertical asymptotes).
- \* Step 4: Find the horizontal or slant asymptotes, if any.
- \* Step 5: Find the intervals on which  $R$  is above the  $x$ -axis and the intervals on which  $R$  is below the  $x$ -axis.  
[Hint: pick a point between the zeros obtained from both the numerator and the denominator.]
- \* Step 6: Graph the asymptotes, if any, plot the points, connect the points and graph  $R$ .

Analyze the graph of each function by following Step 1 through 6 above.

$$1) R(x) = \frac{2x-10}{x-5} = \frac{2(x-5)}{x-5}$$

$$D: \{x | x \neq 5\}$$

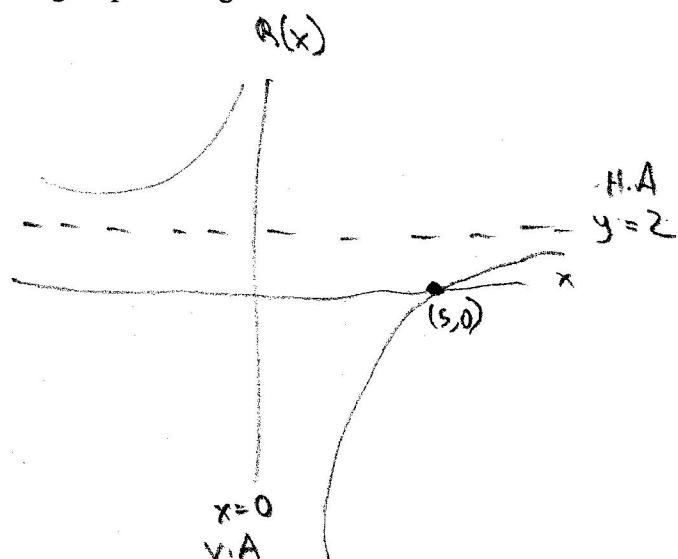
$$x\text{-int: } (5, 0)$$

$$y\text{-int: None}$$

$$V.A: x=5$$

$$H.A: y=2$$

$$\begin{array}{c} R(-1)=-12 \quad R(1)=-8 \quad R(6)=\frac{1}{3} \\ \hline + \quad - \quad 0 \quad + \end{array}$$



$$2) R(x) = \frac{x^2-25}{x-5} = 0$$

$$D: \{x | x \neq 5\}$$

$$x\text{-int: } (x-5)(x+5)=0 \\ \cancel{x=5} \text{ or } x=-5$$

$$y\text{-int: } (0, 5)$$

$$R(x) = \cancel{(x-5)(x+5)} = x+5$$

$$H.A: \text{None}$$

$$V.A: \text{none}$$

$$R(-6)=-1 \quad R(0)=5 \quad R(6)=11$$

$$\begin{array}{c} + \quad - \quad + \quad 5 \quad + \\ 0 \quad -5 \quad 5 \end{array}$$

